Decoding a black hole; from scrambling to information loss



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Collaborators



Xiao-liang Qi (Stanford)



Daniel Roberts (facebook AI)



Alexei Kitaev (Caltech)

Based on

- Chaos in quantum channels, Pavan Hosur, Xiao-liang Qi, Daniel Roberts, BY (2015)
- Efficient decoding for Hayden-Preskill protocol, BY and Alexei Kitaev (2017)
- Verified quantum information scrambling, [experiment with C Monroe group] (2018)

Can we retrieve a quantum state from a black hole?

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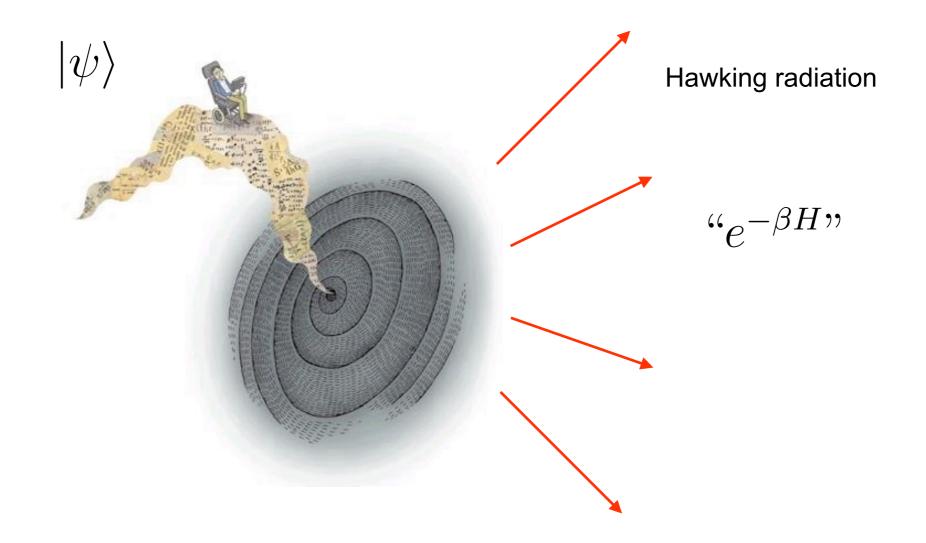
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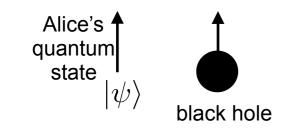
 $|\psi(t)\rangle = e^{-iHt}|\psi(0)\rangle$

(b) General relativity says information is lost in black holes.



Page's thought experiment

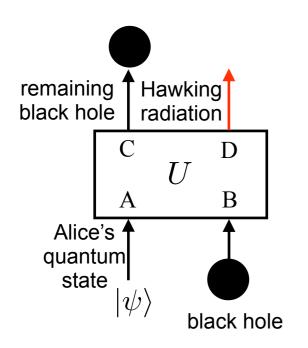
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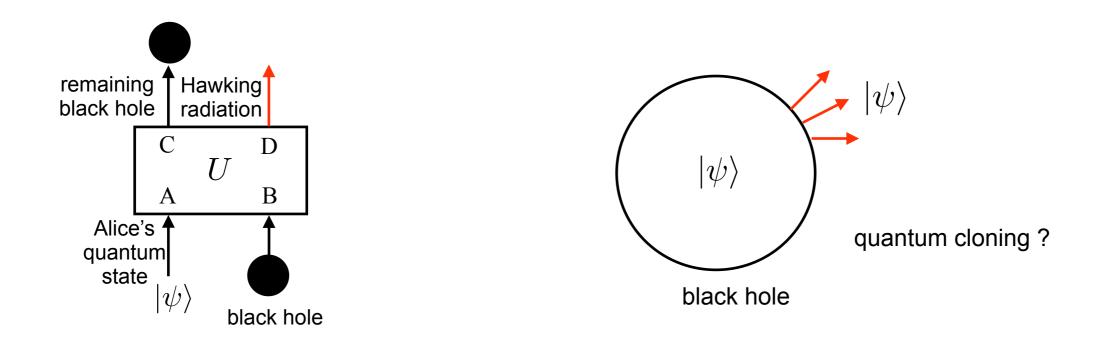


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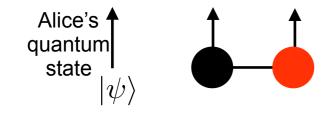
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• Quantum Cloning ? Black hole complementarity ! (no observer can see a quantum cloning).

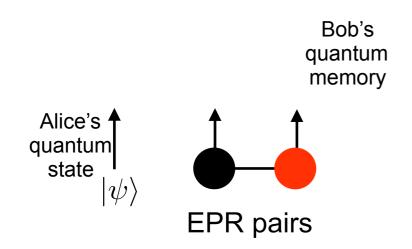


 Bob holds a quantum memory M which is maximally entangled with a black hole (eg. black hole has emitted half of its content).

(eg. eternal AdS black hole).



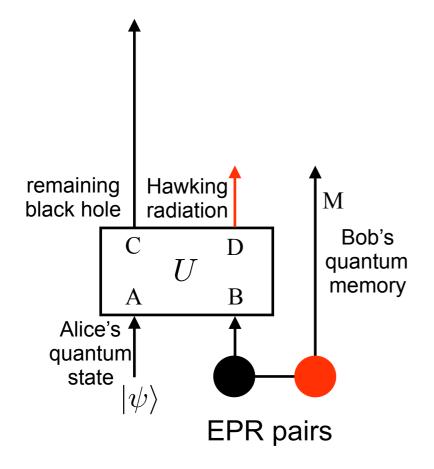
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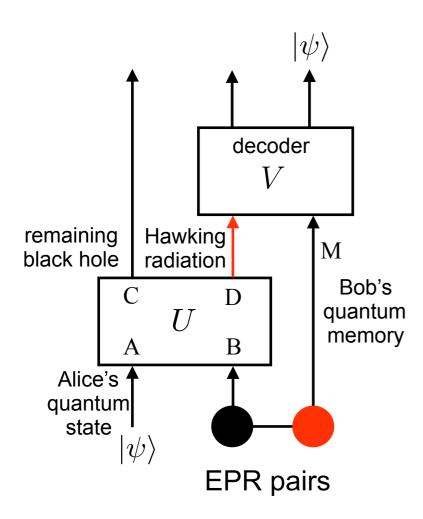
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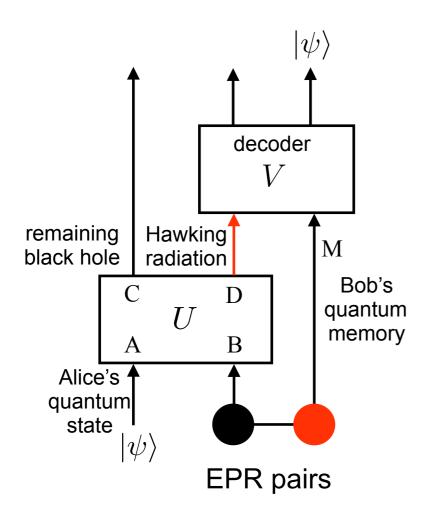
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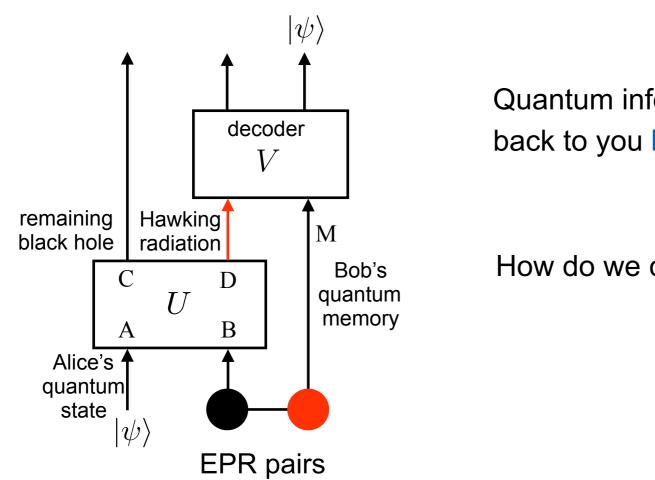
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How do we construct the decoder V ? ▲
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this talk !

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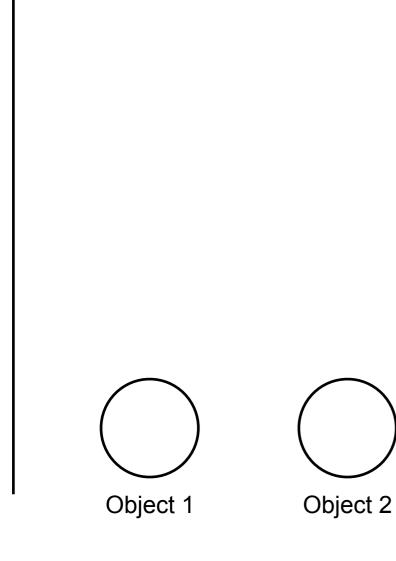
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• Fast scrambling conjecture: Black hole is the "fastest" "scrambler" in nature ? (Hayden-Preskill, Sekino-Susskind, later proven by Maldacena-Shenker-Stanford)

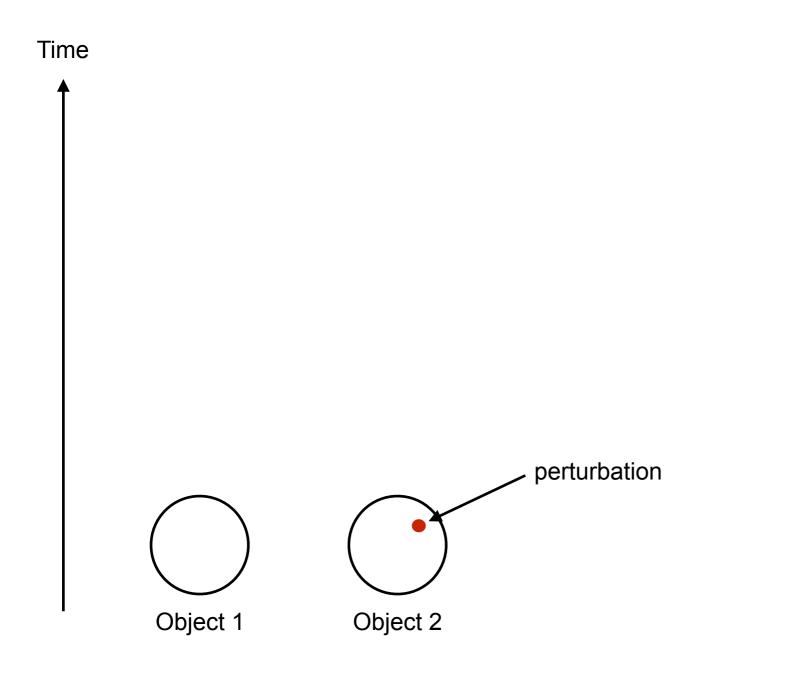
$$t_{\rm scr} \approx \log(n)$$
 ??

• Classical chaos = sensitive dependence of dynamics on initial conditions

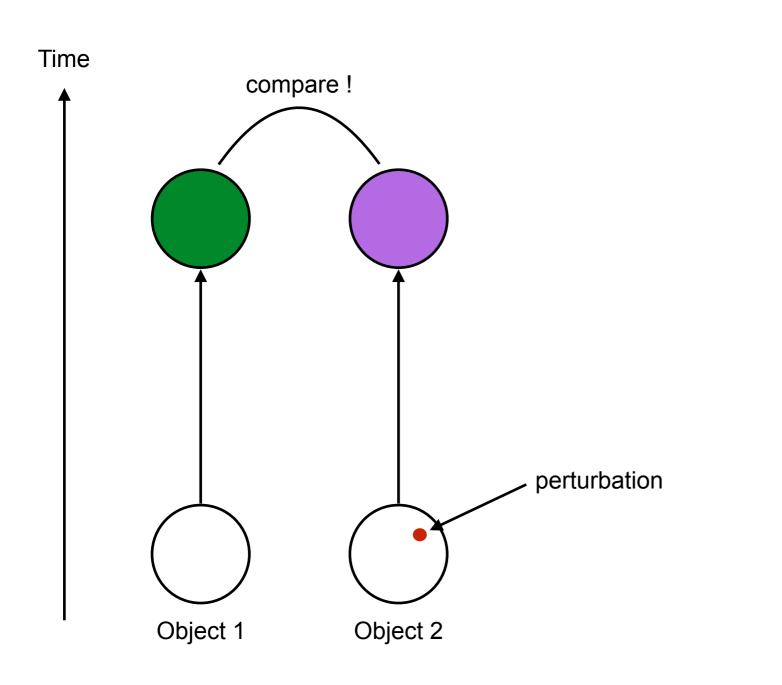


Time

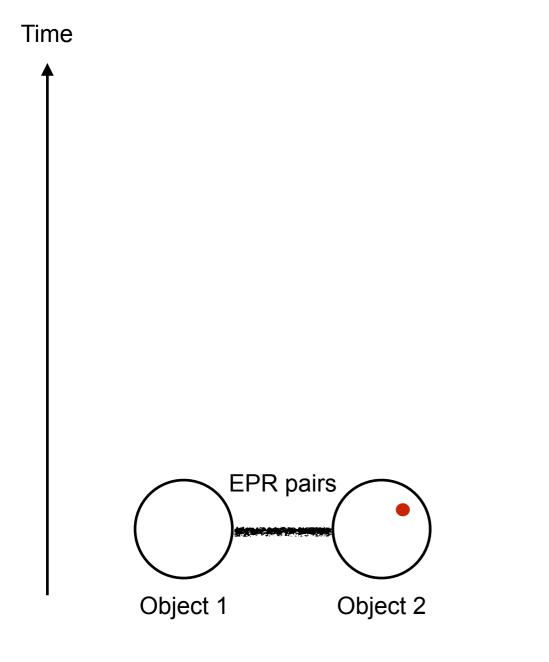
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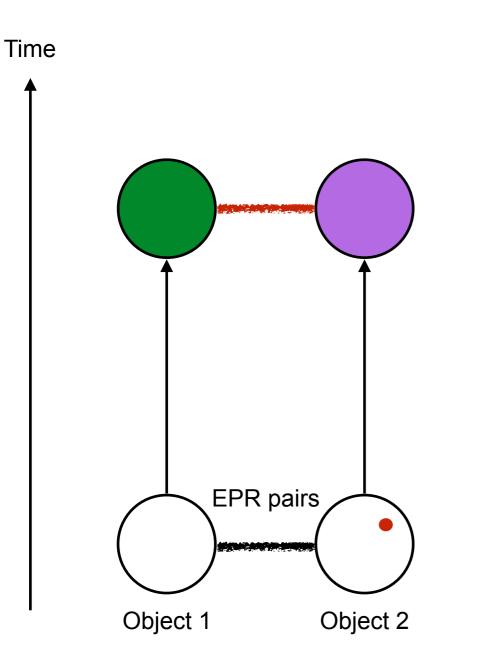
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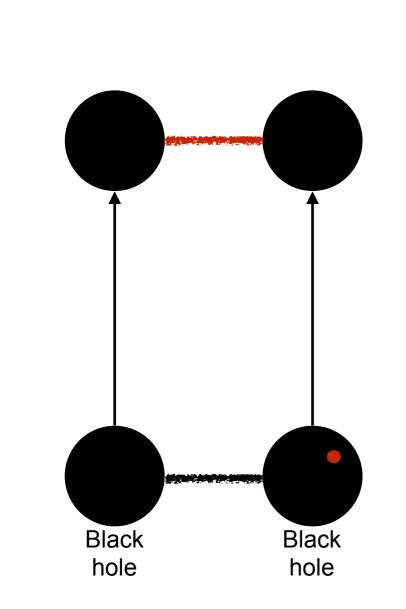


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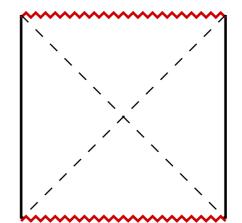
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- Shenker-Stanford: Butterfly effect in an entangled black hole.

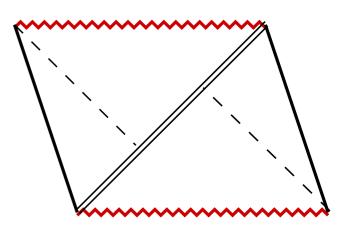
Time



• Perturbation becomes a gravitational shockwave

('t Hooft-Dray 85) ('t Hooft 87, Kiem-Verlinde-Verlinde 95)



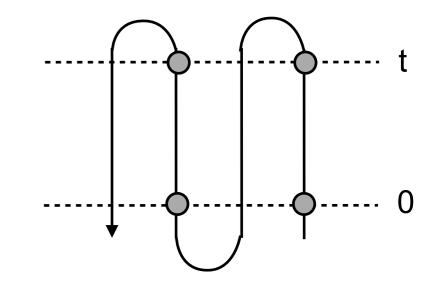


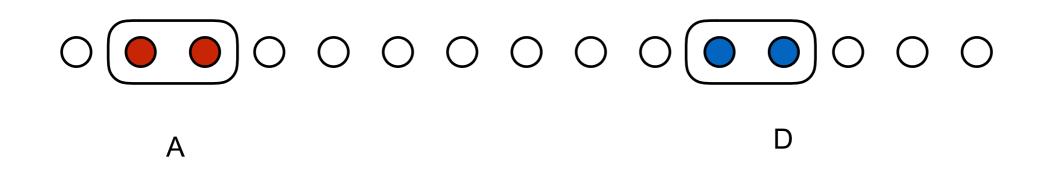
Out-of-time ordered correlation functions (2014)

• OTOCs: $\langle O_A O_D(t) O_A O_D(t) \rangle = \operatorname{Tr} \left(O_A O_D(t) O_A O_D(t) \rho_\beta \right)$

 $O_D(t) = e^{-iHt} O_D e^{iHt}$

Infinite temperature





[Shenker-Stanford, Roberts-Stanford-Susskind, Kitaev]

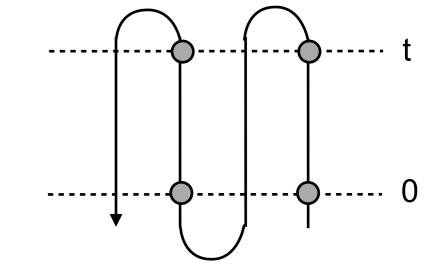
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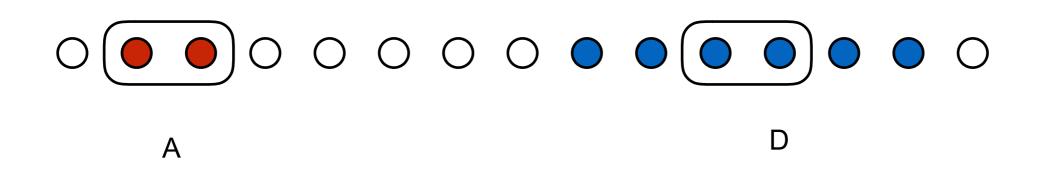
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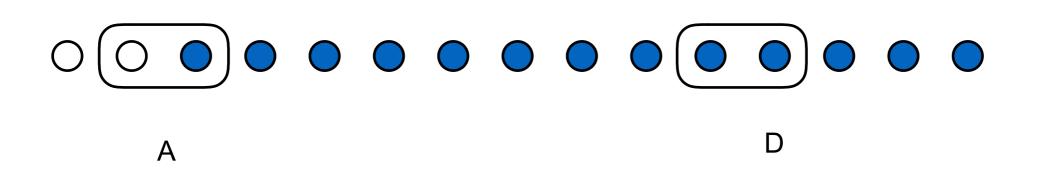
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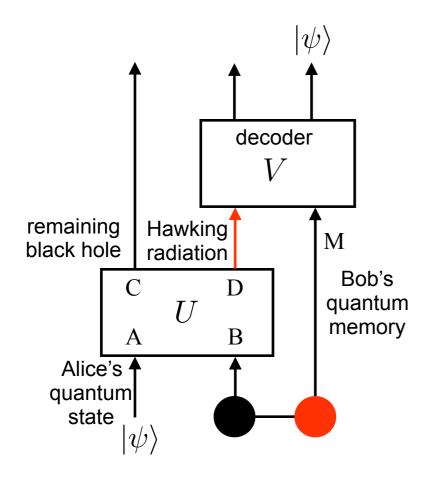
large t $O_D(t)$ becomes a non-local operator OTOC ~ 0

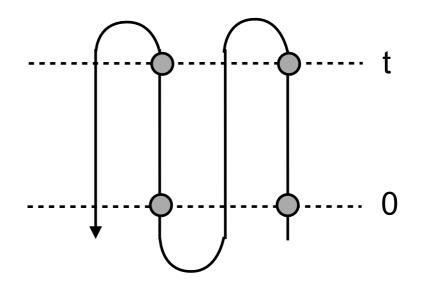
Two operators become non-commuting.



[Shenker-Stanford, Roberts-Stanford-Susskind, Kitaev]

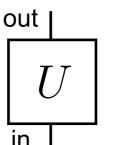
Hayden-Preskill and OTOC?



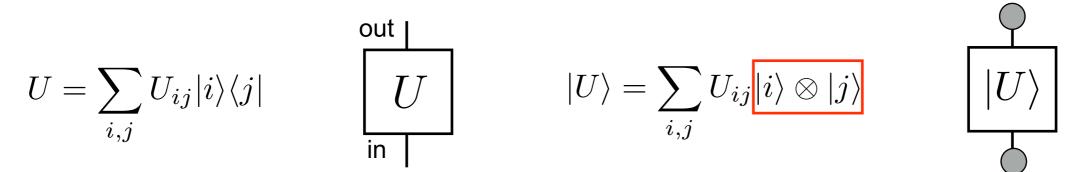


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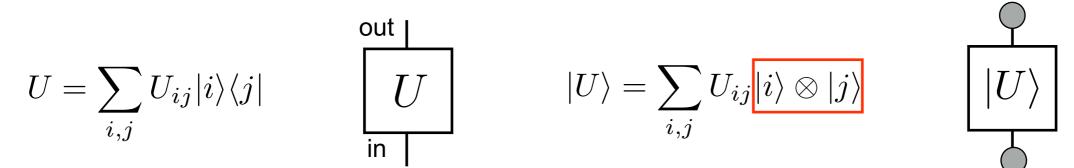
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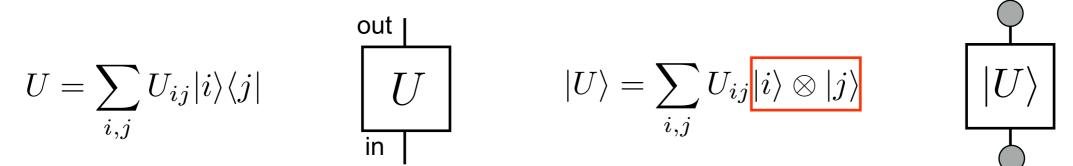


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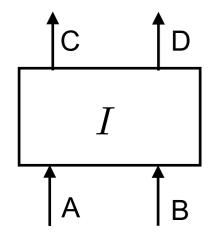


A dynamics can be studied via properties of entanglement !

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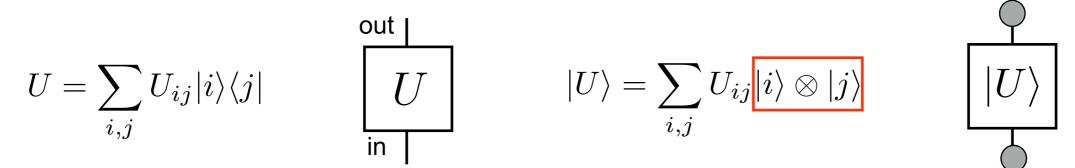


• An identity operator

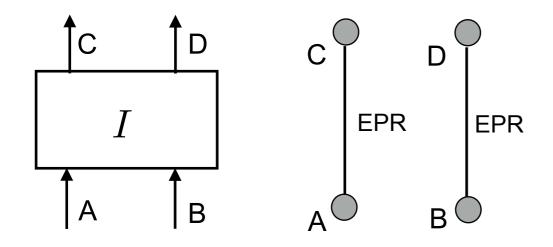


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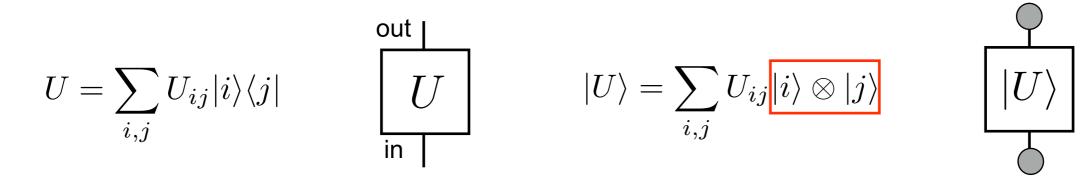


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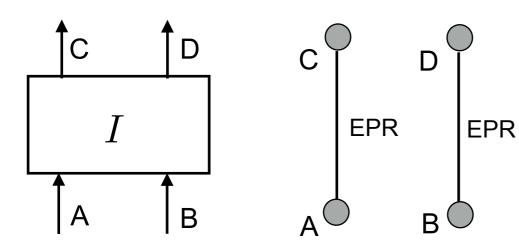


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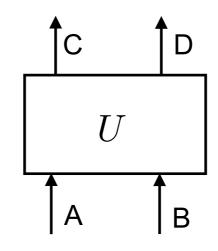
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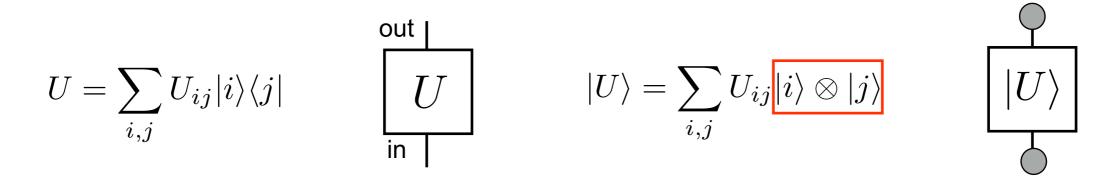


• "Scrambling" and/or "Interacting"

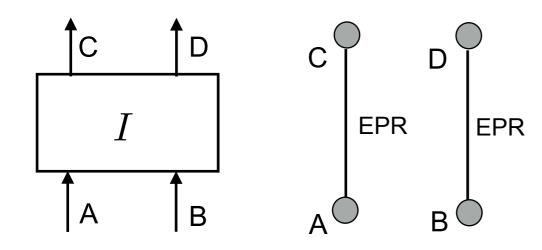


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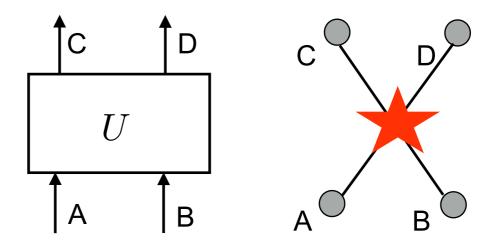
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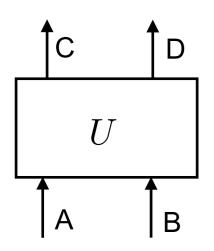
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Multipartite entanglement

• Physical realization ?



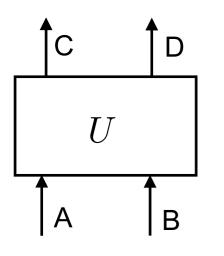
$$U = \sum_{i,j} U_{ij} |i\rangle \langle j|$$
$$|U\rangle = \sum_{i,j} U_{ij} |i\rangle \otimes |j\rangle$$

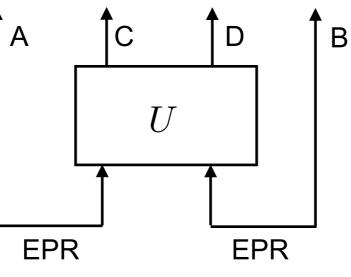
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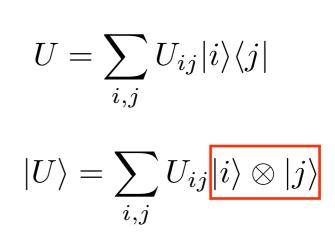
[Hosur-Qi-Roberts-BY]

Multipartite entanglement

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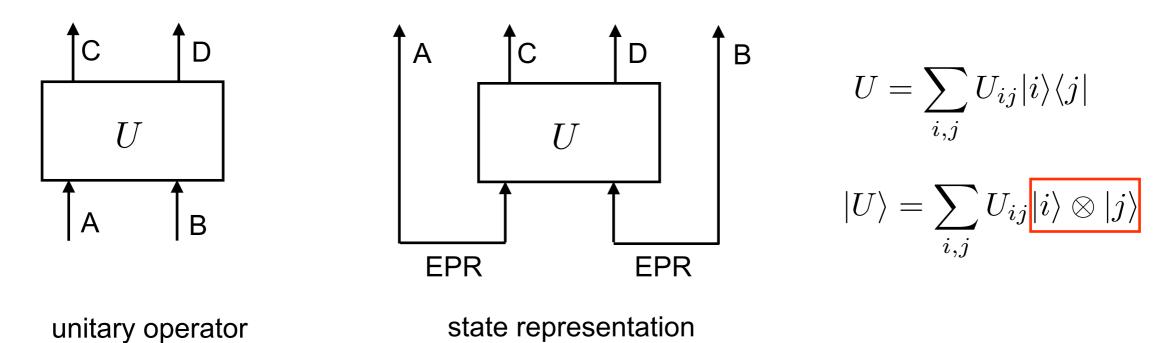


unitary operator

state representation

Multipartite entanglement

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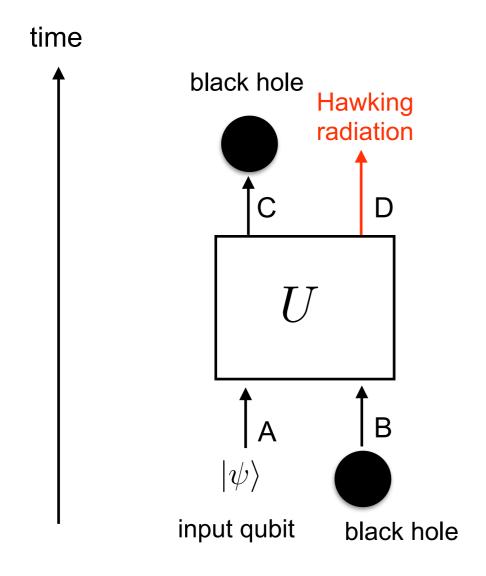


• Multipartite entanglement (Tripartite mutual information)

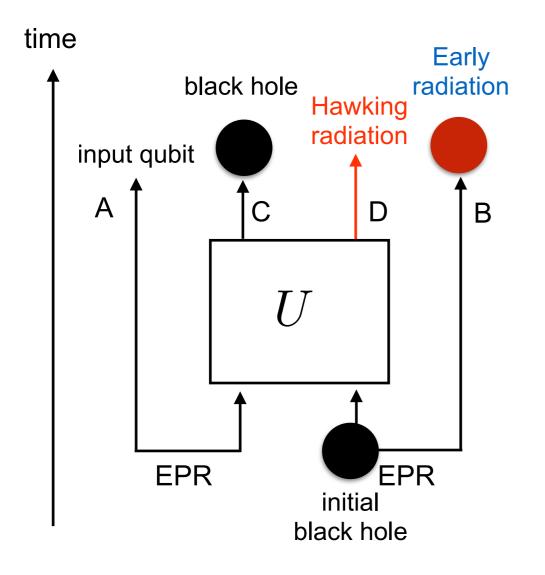
$$I_3 = S_A + S_B + S_C - S_{AB} - S_{BC} - S_{CA} + S_{ABC}$$

- Non-interacting (eg free boson) $I_3 \simeq 0$
- Interacting (eg Haar, late-time) $I_3 \simeq O(n)$

• Viewing the black hole dynamics as a quantum state. (also Hartman-Maldacena 2013)

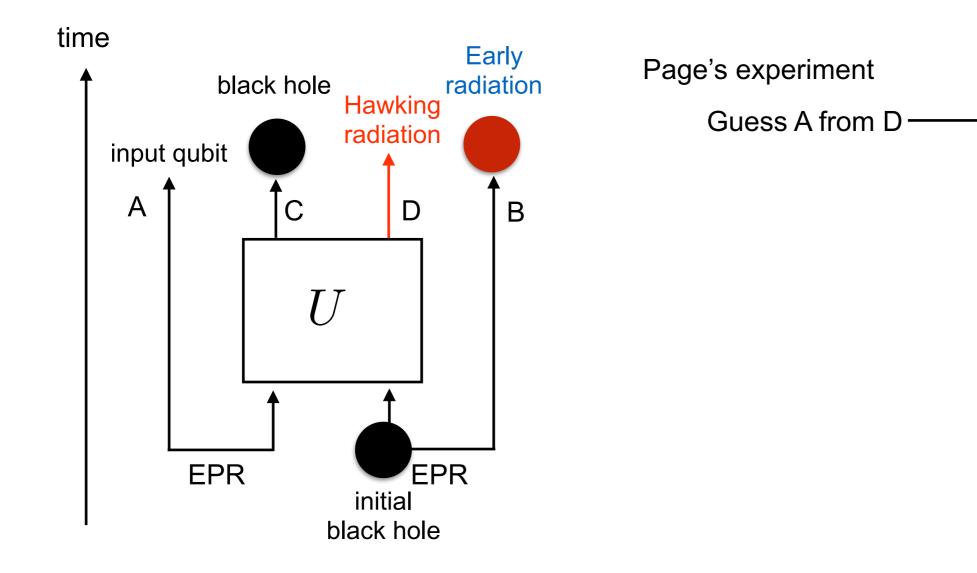


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Mutual information I(A,B) = SA + SB - SAB.

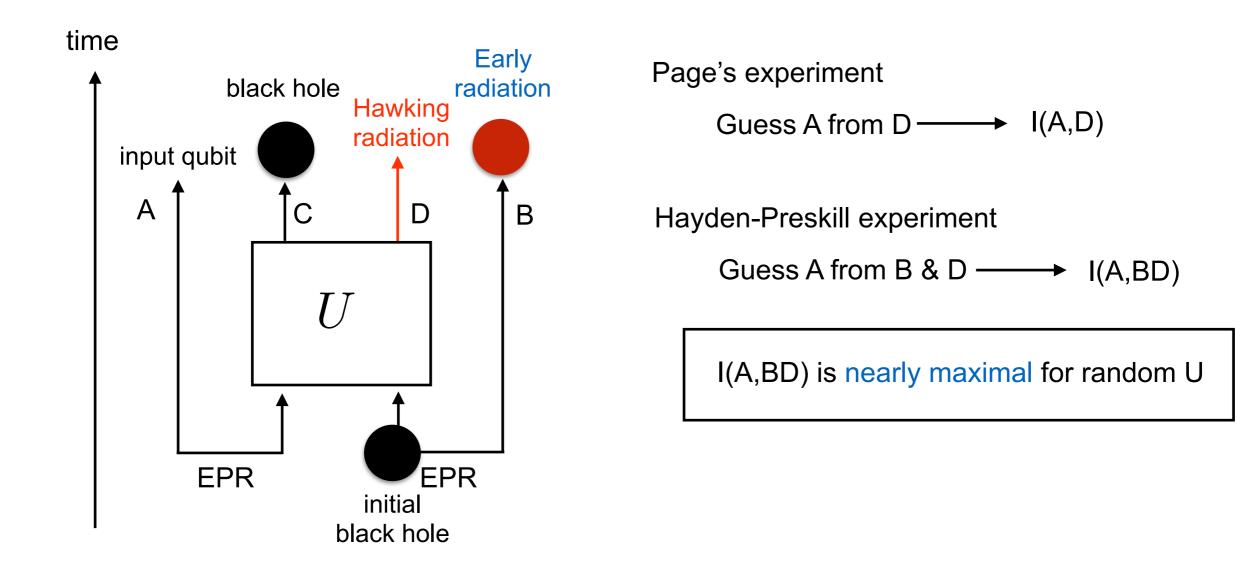
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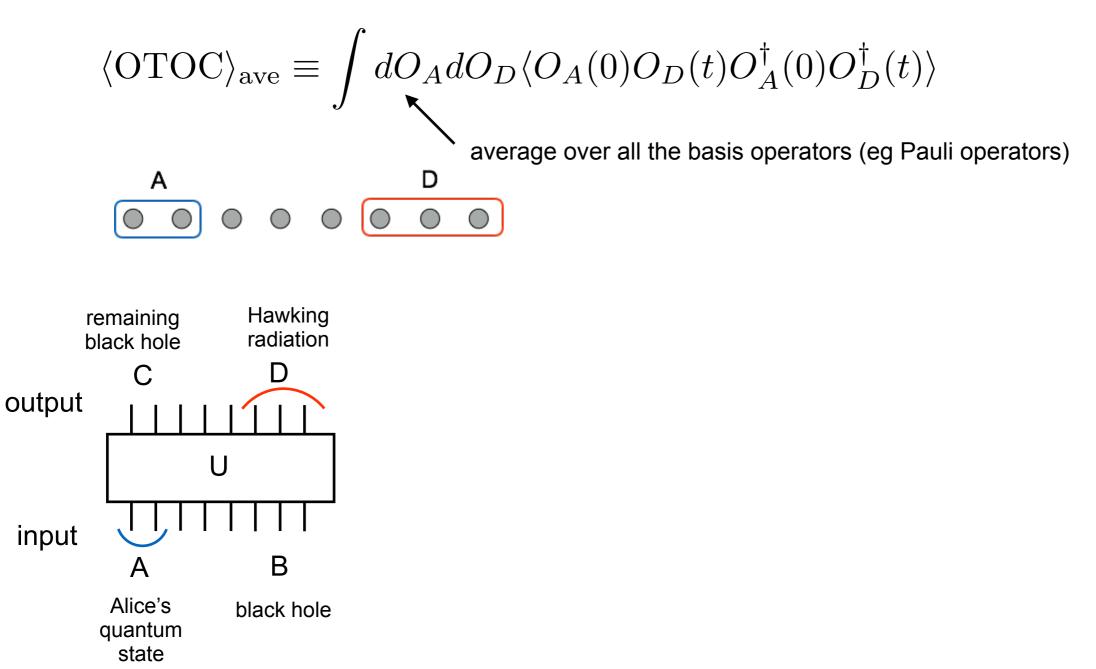
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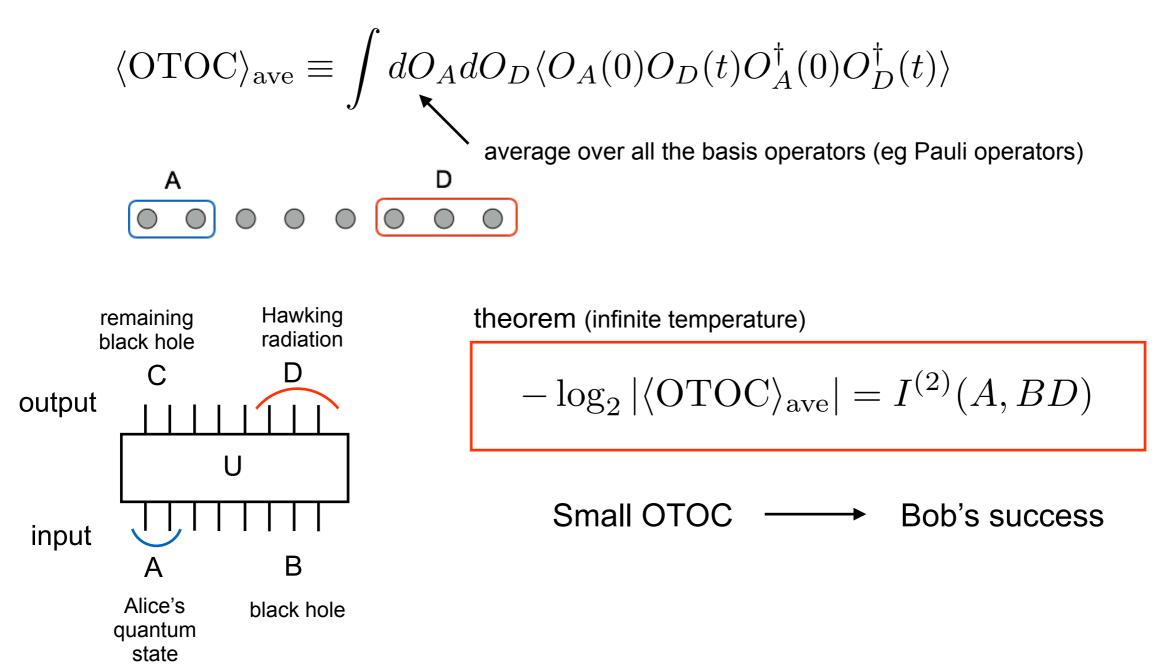
OTOC and Hayden-Preskill

• The averaged OTOCs [with Hosur, Qi and Roberts]



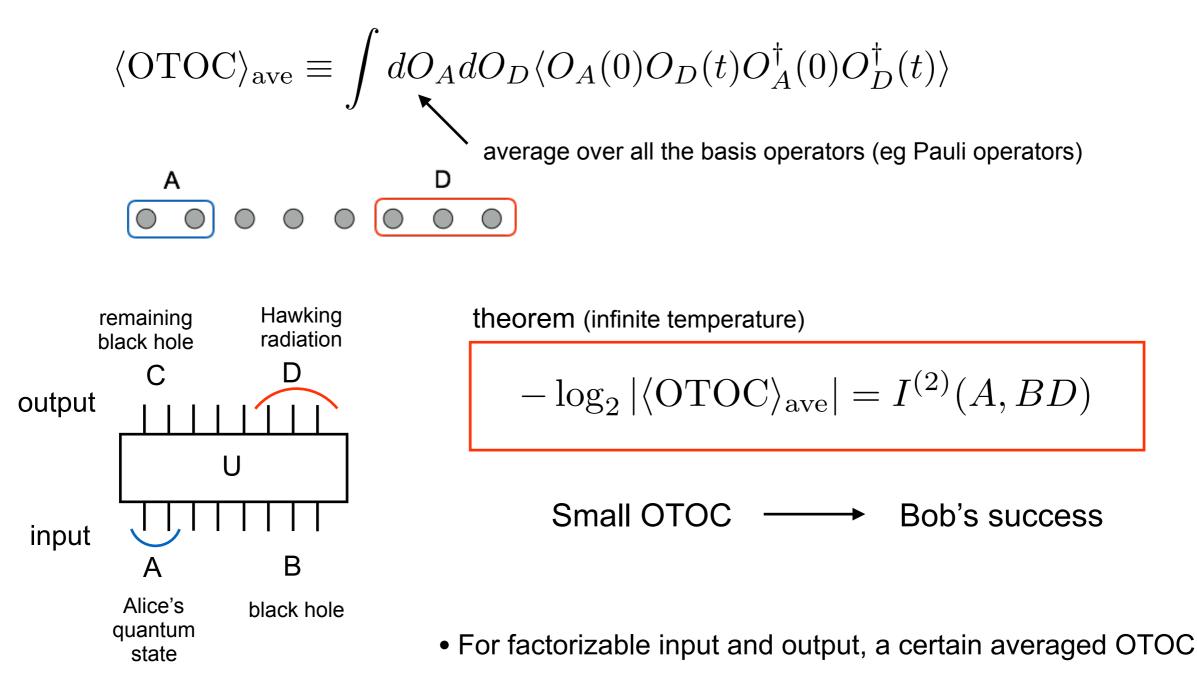
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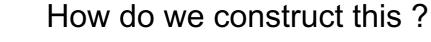
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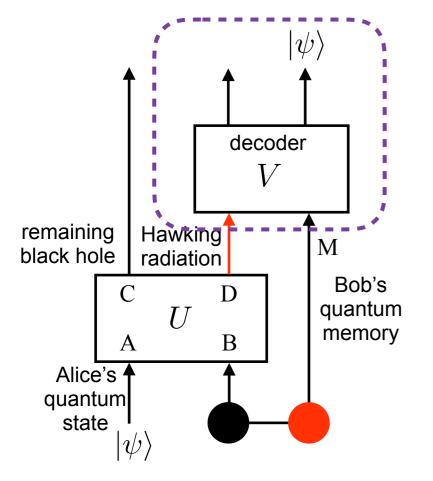
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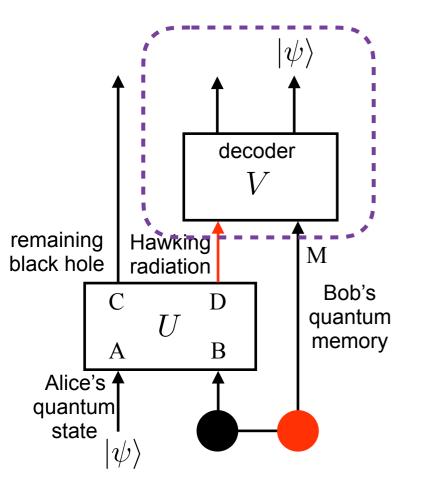
is related to (Sandwiched) Renyi-2 divergence.

Can we really decode the Hawking radiation?





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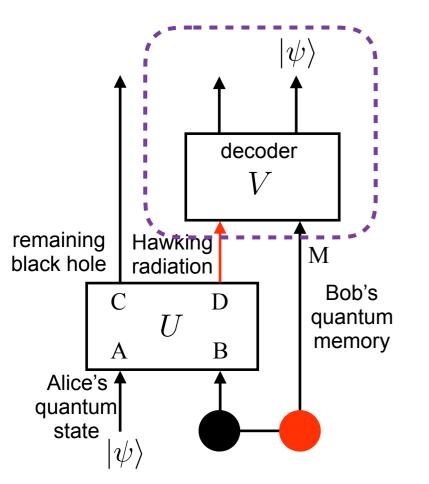
How do we construct this ?

• Simple decoders (with Kitaev)

Version 1 : very simple, but probabilistic. traversable wormhole.

Version 2 : a bit involved, but deterministic.

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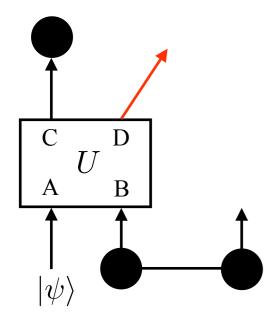
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Crucial assumption

= EPR pairs

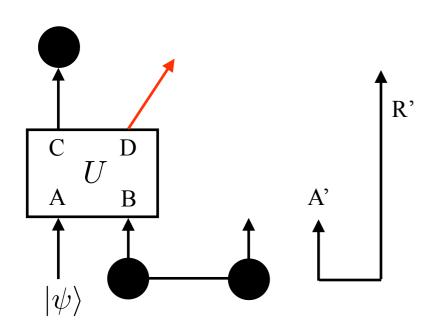
 $\frac{1}{\sqrt{d}}\sum_{i=1}^{u}|j\rangle$ $\otimes |j
angle$

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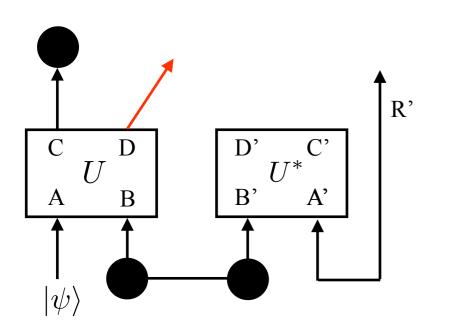
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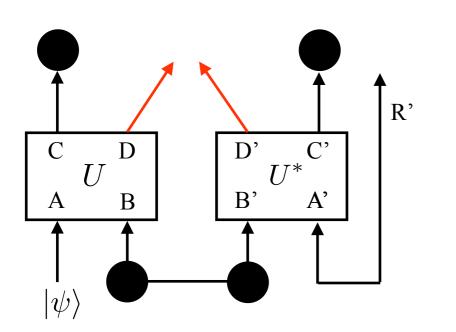


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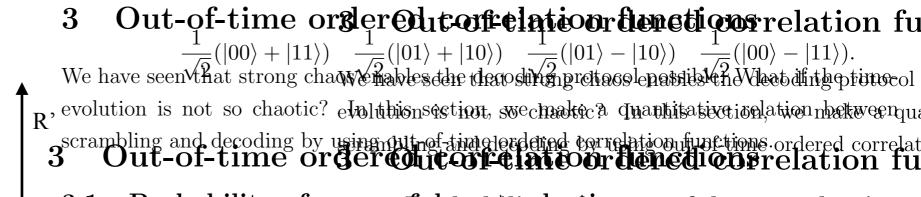
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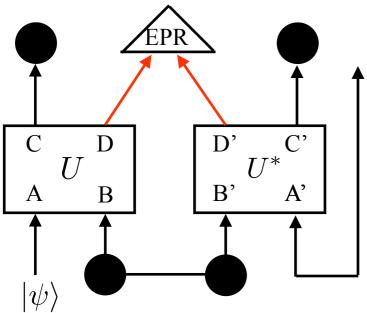


We have seen that strong chaowe have seen that strong chaos that strong chaowe have seen that strong chaowe have seen that strong chaos that strong chaos that strong chaos the set of the strong chaos the set of the strong chaos the set of the

evolution is included in the condition of the section of the sect

3.1 Probability of suggess Propasti-selection for cessful post-selection The probability of measuring The probability of measuring $|EPR\rangle_{DD'}$ is given by

After the time-evolution, one haver the time-evolution, one has Notes on classifica $(\Psi|0|) \otimes \Psi_{D} \otimes$



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EPR

С

А

 $|\psi
angle$

D

В

U

D'

B'

С'

A'

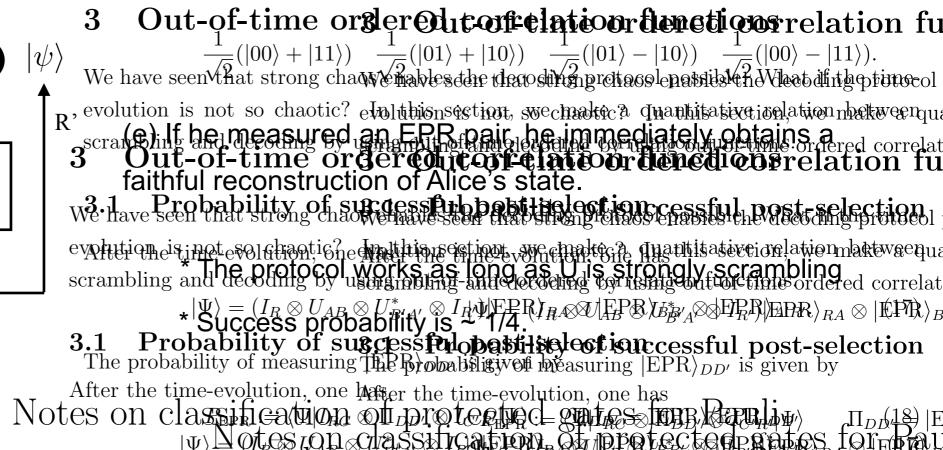
 U^*

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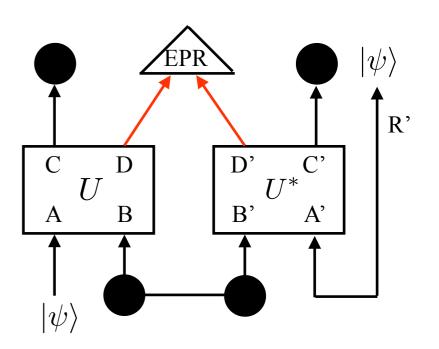


Reconstruction probabilities

- Decoding protocol crucially relies on "scrambling".
- Probability of measuring an EPR pair

$$P_{\rm EPR} = 2^{-I^{(2)}(A,BD)} = \langle OTOC \rangle_{\rm ave} \approx \frac{1}{d_A^2}$$

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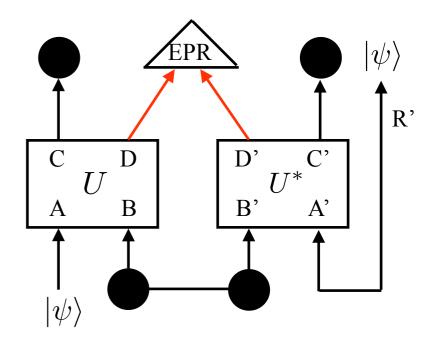
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The probability decreases as the message size d_A increases....

• Probability of successful teleportation (measured by fidelity)

$$F_{\rm EPR} = \frac{2^{I^{(2)}(A,BD)}}{d_A^2} = \frac{1}{d_A^2 \langle OTOC \rangle_{\rm ave}} \approx 1$$

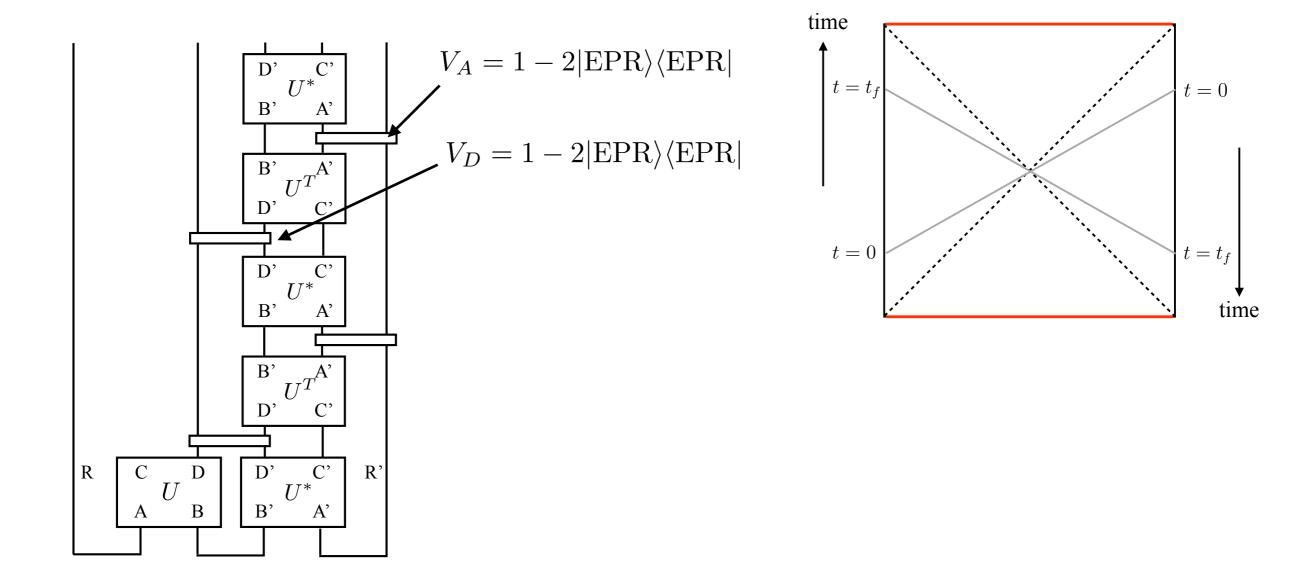
If maximally chaotic, then the fidelity is unity.

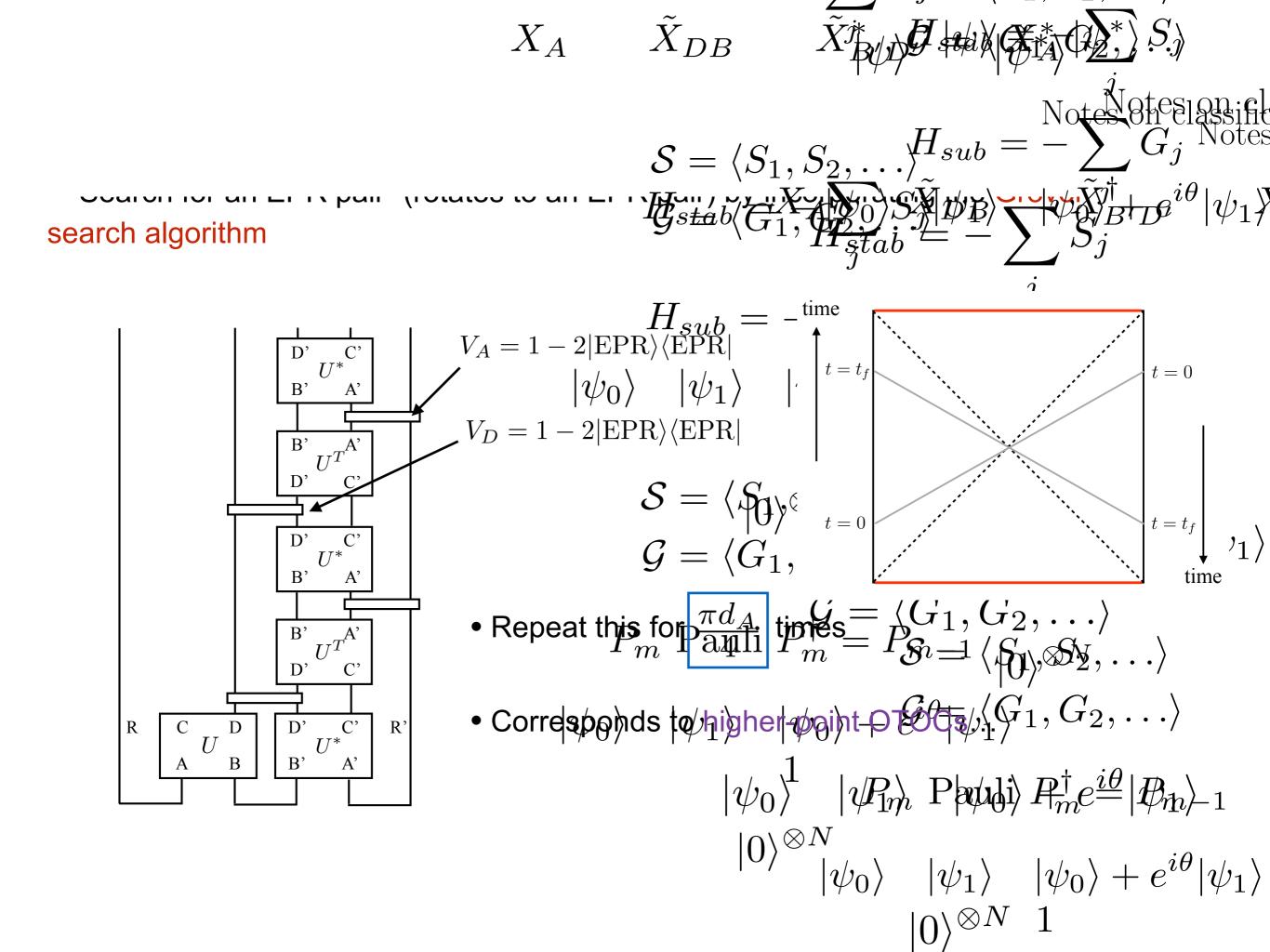


Deterministic decoding protocol

Notes 8 hestesis

• "Search for an EPR pair" (rotates to an EPR pair) by incorporating the Grover search algorithm



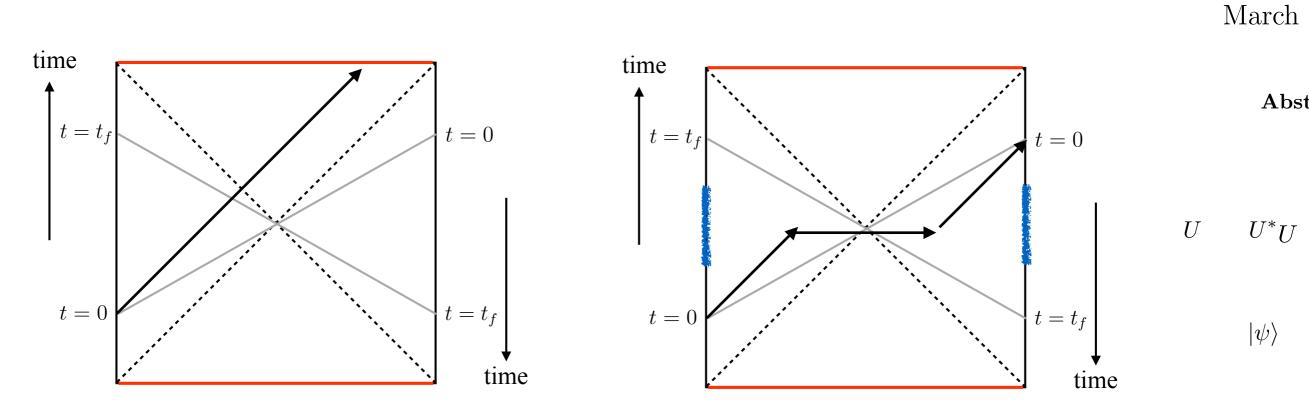


Traversable wormhole in AdS black hole ?

• By coupling the left and right boundary appropriately, a wormhole becomes traversable [Gao-Jafferis-Wall, Maldacena-Stanford-Yang]

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Notes on

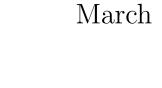


 $H_{stab} =$

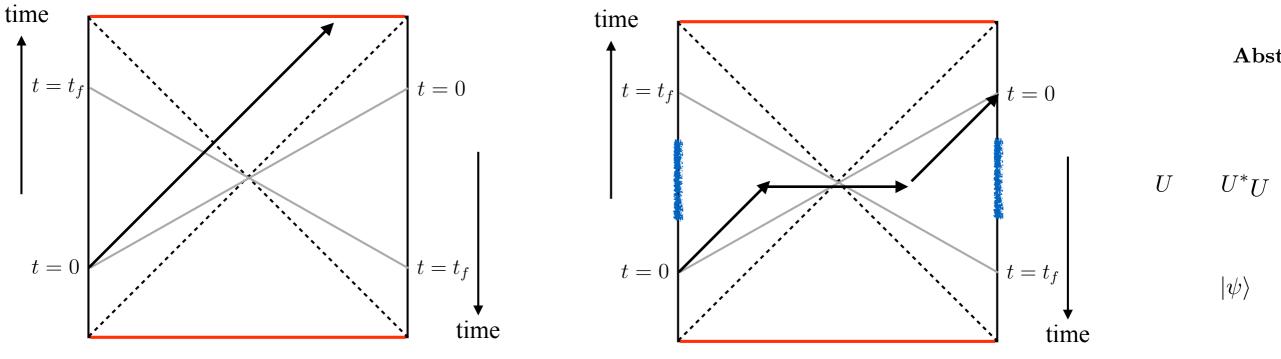
Traversable wormhole in AdS black hole ?

• By coupling the left and right boundary appropriately, a wormhole becomes traversable [Gao-Jafferis-Wall, Maldacena-Stanford-Yang]

• Decoder for Hayden-Preskill may be interpreted as a traversable technologies interpreted as a traversable techno



Notes on



 $H_{stab} =$

Holographic interpretation ?

• Reverse the time direction !

of double trace **cheforitietismend** is the deformation of the bulk which formation sends negative energy on the bulk which a send of the bulk which the high energy on the bulk which and the bulk which and the bulk which and the bulk which and the bulk which a send of the bulk which a send of the bulk which and the bulk which and the bulk which and the bulk which are opens up for a while. Under this deformation, a set to be a while. Under this deformation, a set to be a while. Under this deformation, a set to be a while. Under this deformation, a set to be a while. Under this deformation, a set to be a while. Under this deformation, a set to be a while bulk which a set to be a while. Under the bulk which are a set to be a while bulk which a set to be a s

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Holographic interpretation ?

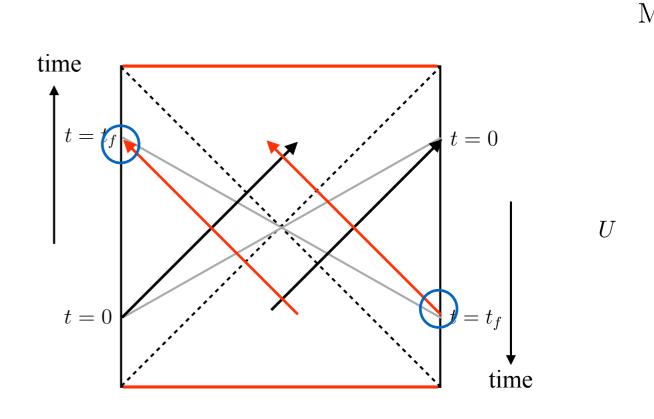
• Reverse the time direction !

Notes

A,D Infalling/outgoing radiations

B,C field modes and high energy things

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Holographic interpretation?

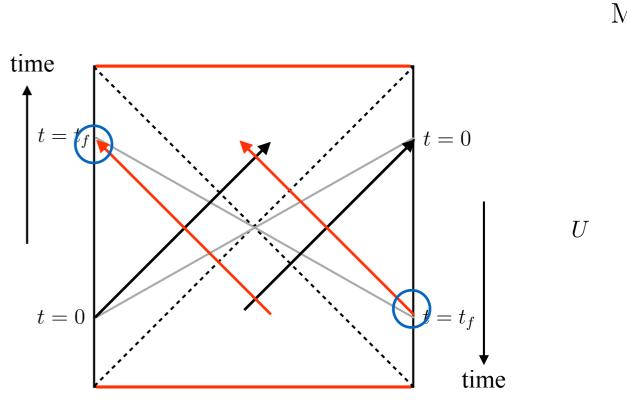
Reverse the time direction !

- Projection onto an EPR pair makes the wormhole traversable?

A,D Infalling/outgoing radiations

B,C field modes and high energy things

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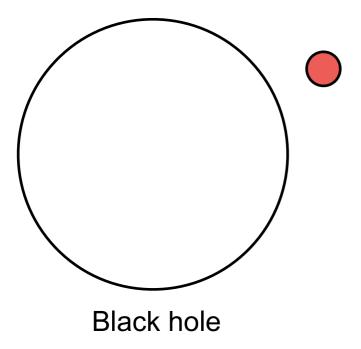
Notes

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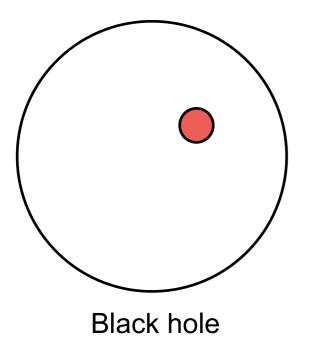
• We should update "black hole complementarity".

- There is no quantum cloning. An object can be pulled back from a black hole !



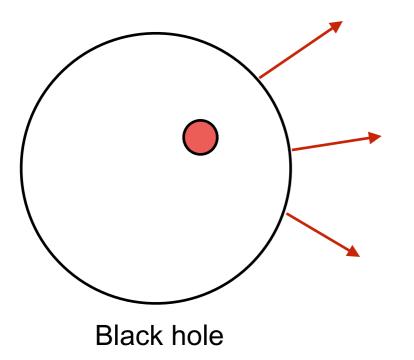
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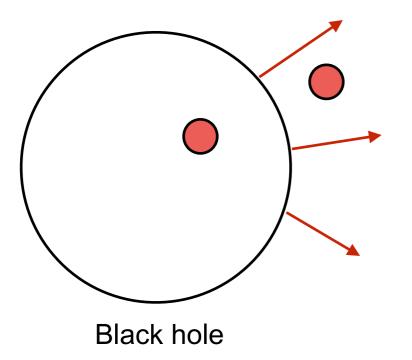
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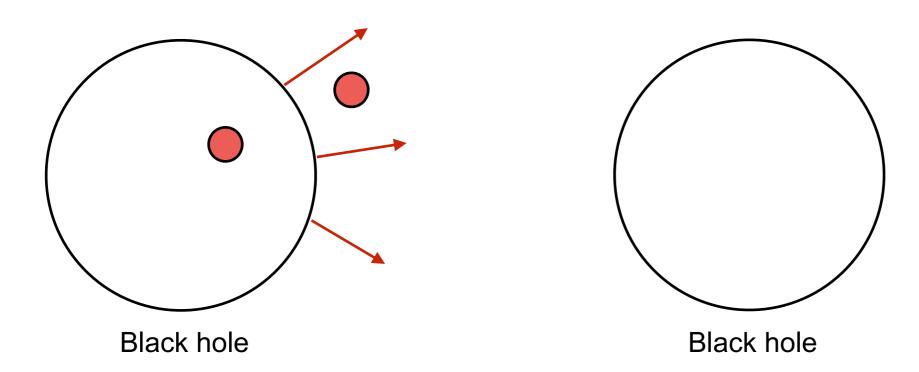
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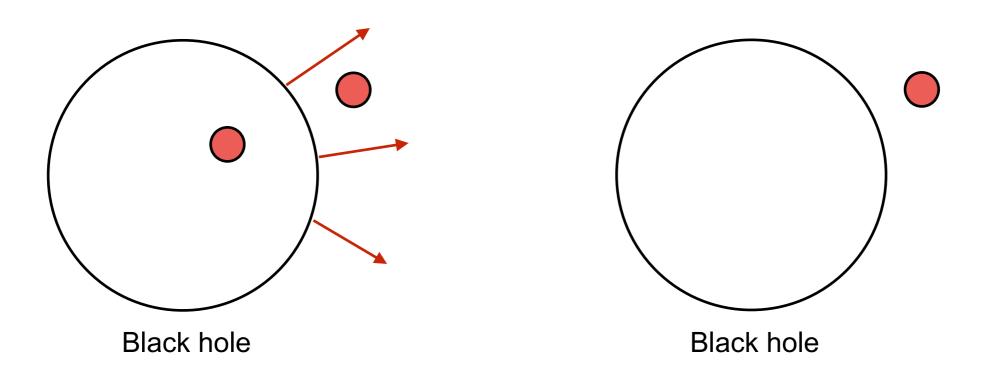
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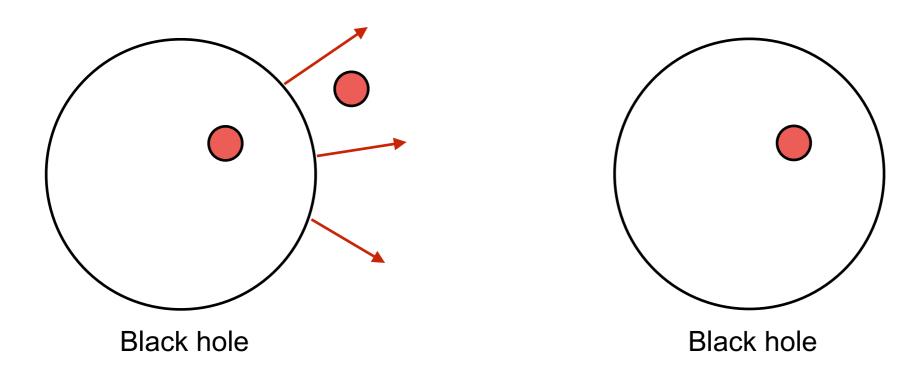
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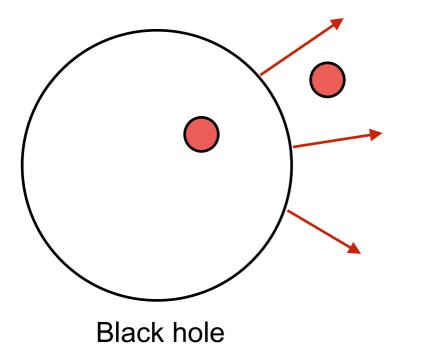
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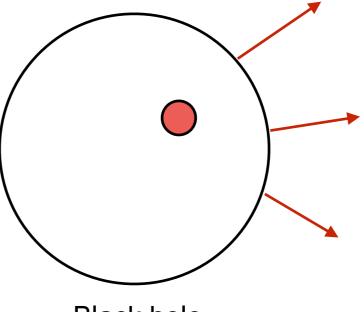


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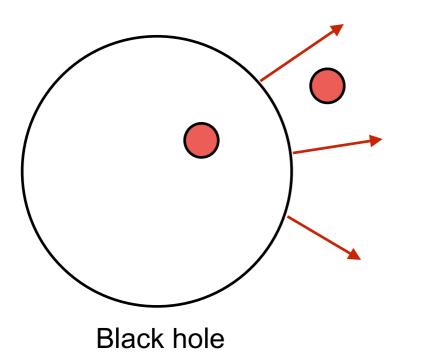
Black hole

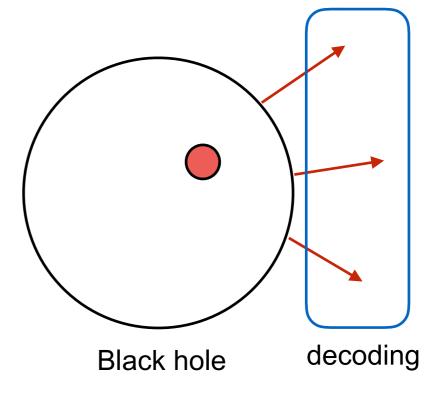
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previously....

modern interpretation



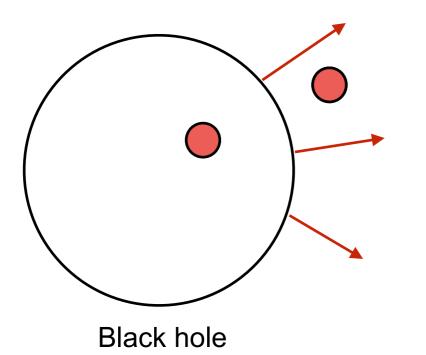


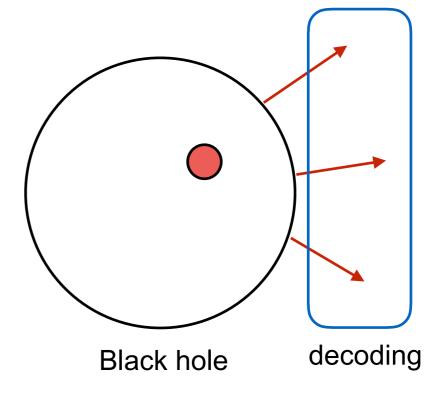
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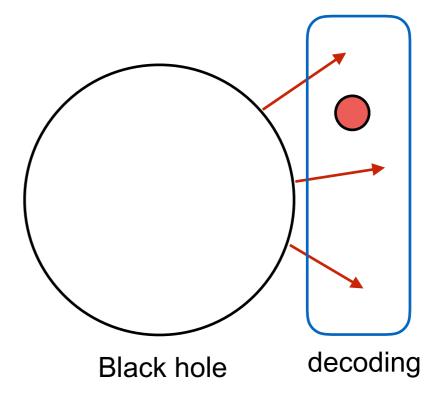


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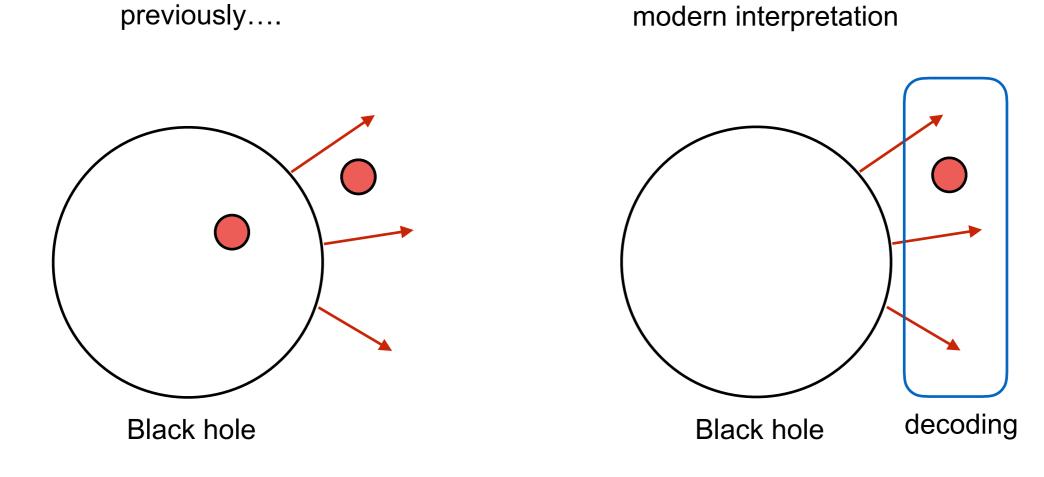
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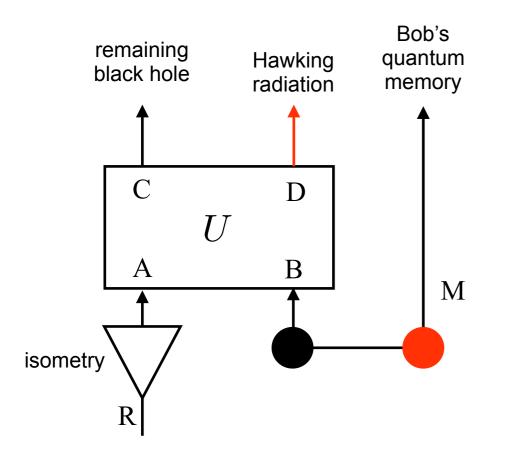
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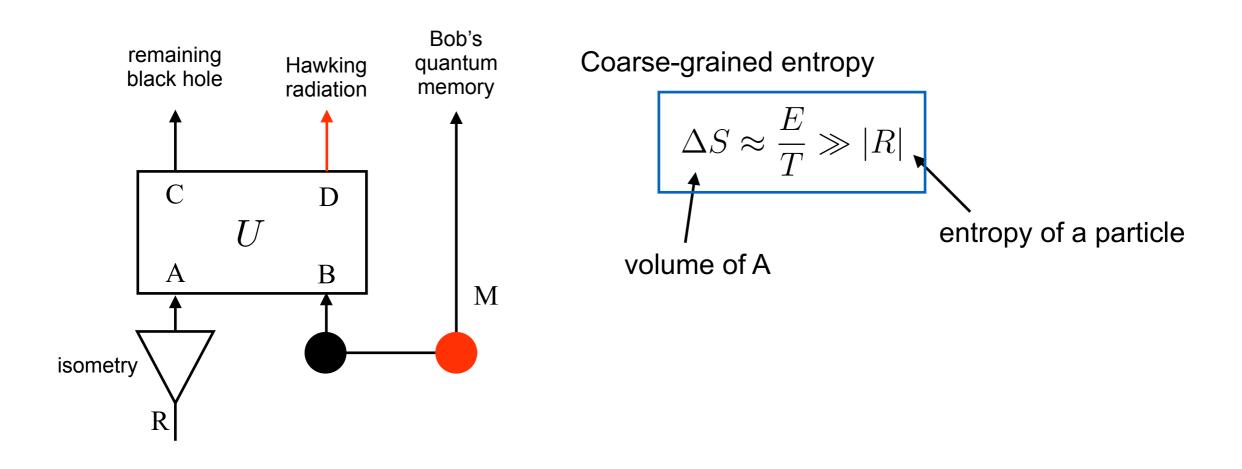


• We can probe the black hole interior !?

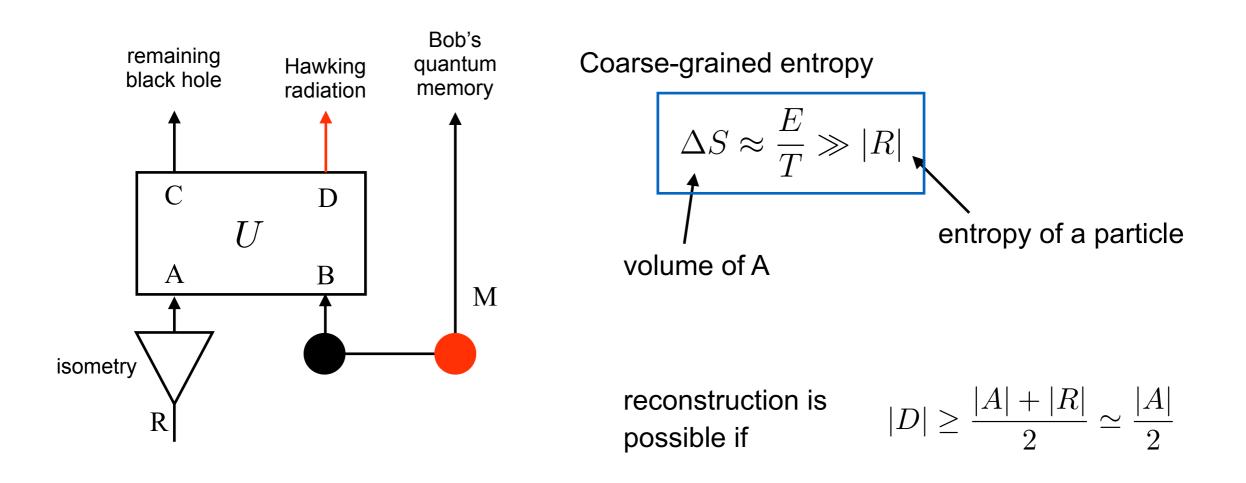
• A particle with energy E, carrying R qubits information, falls into a black hole at temperature T.



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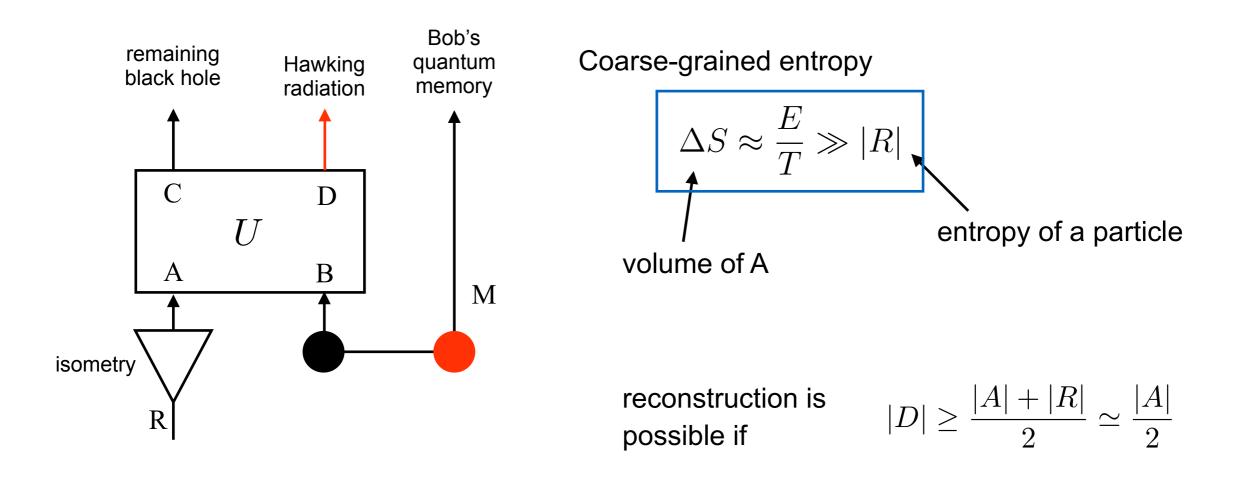


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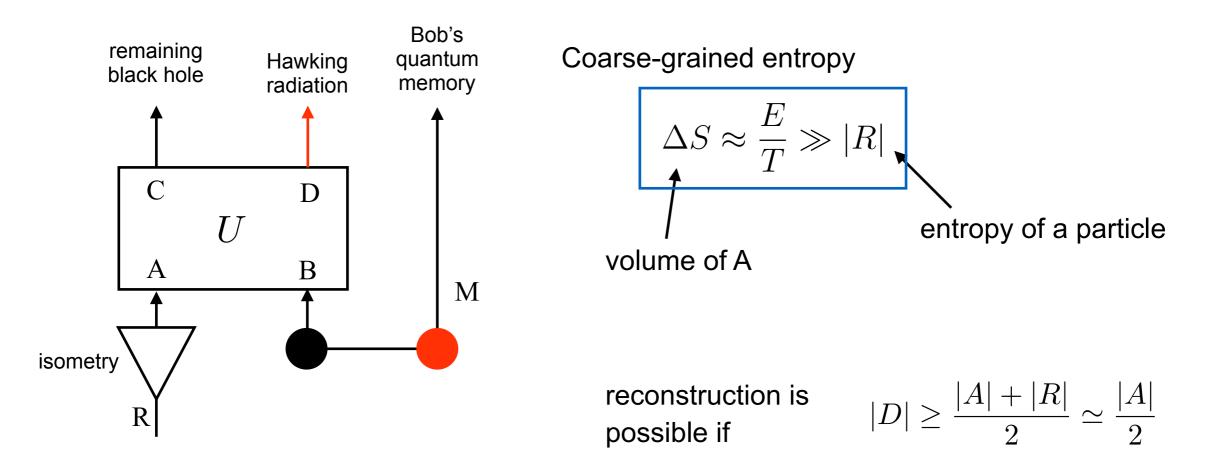


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• A closely related idea was used to resolve the firewall paradox (Verlinde-Verlinde)

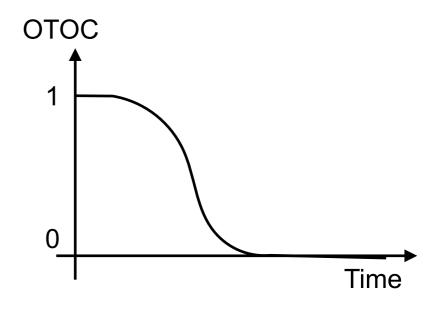


- A particle with energy E, carrying R qubits information, falls into a black hole at temperature T.
- A closely related idea was used to resolve the firewall paradox (Verlinde-Verlinde)
- In QI literature, a similar idea has been recently proposed. "alpha-bits" (Hayden-Pennington)



Experimental characterization of scrambling

• OTOC decay due to decoherence...



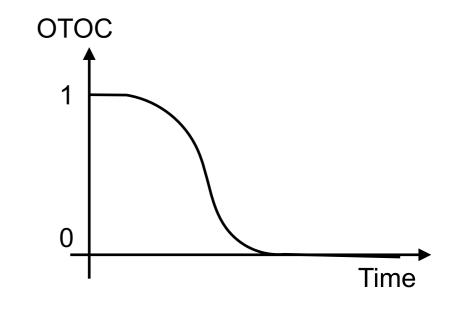
double trace deformations which couple two CFTs. formation sends negative energy on the bulk which sole opens up for a while. Under this deformation, a the right boundary.

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Experimental characterization of scrambling

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agations. project outgoing Hawking radiations onto the high taken hole and reaches the righthand It aisers ableavia postselection. It is unclear If U = unitary + decoherence, ...

EPR projection

PEPR : OTOC decay with scrambling and decoherence

Decoding fidelity

FEPR : OTOCs with scrambling only

With Chris Monroe group at U Maryland

arXiv:1806.02807

Verified Quantum Information Scrambling

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Quantum scrambling is the dispersal of local information into many-body quantum entanglements and correlations distributed throughout the entire system. This concept underlies the dynamics of thermalization in closed quantum systems, and more recently has emerged as a powerful tool for characterizing chaos in black holes [1–5]. However, the direct experimental measurement of quantum scrambling is difficult, owing to the exponential complexity of ergodic many-body entangled states. One way to characterize quantum scrambling is to measure an out-of-time-ordered correlation function (OTOC); however, since scrambling leads to their decay, OTOCs do not generally discriminate between quantum scrambling and ordinary decoherence. Here, we implement a quantum circuit that provides a positive test for the scrambling features of a given unitary process [6, 7]. This approach conditionally teleports a quantum state through the circuit, providing an unambiguous litmus test for scrambling while projecting potential circuit errors into an ancillary observable. We engineer quantum scrambling processes through a tunable 3-qubit unitary operation as part of a 7-qubit circuit on an ion trap quantum computer. Measured teleportation fidelities are typically $\sim 80\%$, and enable us to experimentally bound the scrambling-induced decay of the corresponding OTOC measurement.

Decoding a black hole; from scrambling to information loss



Beni Yoshida (Perimeter Institute)

August 2018 @ Tokyo